## Spin-orbit influence on $d_{z^2}$ -type surface state at Ta(110)

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The influence of spin-orbit interaction on an occupied surface state at Ta(110) is investigated with spin- and angle-resolved photoemission and electronic structure calculations. The surface state appears in a symmetry gap at a binding energy of 0.45 eV at  $\overline{\Gamma}$  and exhibits a free-electron-like  $E(\mathbf{k}_{\parallel})$  dispersion with an effective mass  $m^*/m_e$  of about -1.35 along  $\overline{\Gamma}$   $\overline{H}$ . Photoemission results for excitation with s- and p-polarized light confirm the predicted  $d_{z^2}$ -type symmetry of the state close to  $\overline{\Gamma}$ . Spin-resolved data for finite  $\mathbf{k}_{\parallel}$  reveal a pure Rashba-type spin texture with a Rashba parameter of  $0.063 \pm 0.007$  eV Å. These findings clearly prove a sizable impact of spin-orbit coupling on the  $d_{z^2}$  surface state and resolve a longstanding disagreement on this issue.

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Spin-orbit coupling (SOC) is known to affect the electronic structure of solids with heavy elements, in particular, by lifting the spin degeneracy of surface states [1–4]. The resulting Rashba-type spin dependence is locked with the direction of the electron momentum. Tantalum is a heavy element with a pronounced surface state at the (110) surface [5–7]. This state appears just below the Fermi level around the center of the surface Brillouin zone  $\overline{\Gamma}$  within a gap for bulk bands of even symmetry. However, no hybridization with odd-symmetry bulk states was observed and thus no influence of spin-orbit coupling was found in the results [5]. It was concluded that "the spin-orbit interaction does not strongly impact this state" [6]. A predominant  $d_{z^2}$  symmetry character of 93% was calculated for this state around  $\overline{\Gamma}$ , "which accounts for the lack of dispersion" [7].

In contrast, the direct neighbor in the periodic table, tungsten, with the same crystal structure (body-centeredcubic) and a very similar band structure, exhibits a wealth of spin-orbit-induced effects in the surface electronic structure [8–15]. Therefore, spin-orbit effects are expected for Ta as well. Recently, spin-polarized unoccupied surface bands were identified on Ta(110), whose spin dependence originates from SOC [16]. There is apparently substantial impact of SOC in the unoccupied states, which strongly suggests that SOC should influence the occupied states as well. The latter is at variance with earlier claims. To resolve this contradiction, we revisit the occupied  $d_{7^2}$ -type surface state at Ta(110), now using angle-resolved photoelectron spectroscopy (ARPES) with spin detection. The study is of further importance because W(110) has no equivalent to the  $d_{z^2}$ -like surface state of Ta(110) [17]. An explanation for this difference is found in the different energetic positions of the surface states relative to the bulk states, caused by the different lattice constants [16].

Prototypical  $d_{7^2}$ -type surface states are known from the (0001) surfaces of hexagonal-closed-packed lanthanide surfaces. Indications for a spin-orbit-induced Rashba-type splitting, enhanced by an oxygen-induced modification of the surface potential, have been observed by spin-integrated ARPES for Lu (Z = 71) but not for Y (Z = 39) [18]. In the cases of ferromagnetic Gd (Z = 64) and Tb (Z = 65), the magnetic exchange interaction dominates the spin-orbit interaction [18-20]. Nevertheless, a small energy shift of the surface band, asymmetric in  $\mathbf{k}_{\parallel}$ , was observed upon switching the magnetization direction. The shift, observed by spin-integrated ARPES, was attributed to the Rashba splitting. This approach is restricted to ferromagnetic samples. With these results in mind, Ta (Z = 73) is a promising candidate for studying spin-orbit effects on a localized  $d_{z^2}$ -type surface state even on a nonferromagnetic high-Z element directly with spin-resolved ARPES.

The Ta(110) surface was cleaned by repeated cycles of heating in an oxygen atmosphere (in the beginning  $6 \times 10^{-8}$  mbar, later  $1 \times 10^{-8}$  mbar) up to 1800 K and subsequent flashing up to 2700 K [16]. This cleaning procedure was successful in removing contaminants, such as carbon and oxygen, from the surface. The surface quality was confirmed by Auger electron spectra and by a sharp  $(1 \times 1)$  low-energy electron diffraction pattern with low background intensity. The intensity of the surface state under investigation served as the most sensitive criterion for the surface quality [6,21].

The surface electronic structure of Ta(110) was investigated by ARPES with three-dimensional spin sensitivity at the ESPRESSO end station of beamline BL-9B at the Hiroshima Synchrotron Radiation Center (HiSOR) [22]. We used linearly polarized undulator radiation with the electric field vector being either parallel (p polarized) and perpendicular (s polarized) to the plane of incidence, as schematically shown in Fig. 1(a). The angle of light incidence was 50° relative to the lens axis of the electron analyzer. High-resolution ARPES data were obtained using a VG Scienta R4000 display electron analyzer. The energy and angle resolution was <50 meV (<25 meV) and <0.6° (<0.6°) for 43 eV (22 eV) radiation. The spin-resolved

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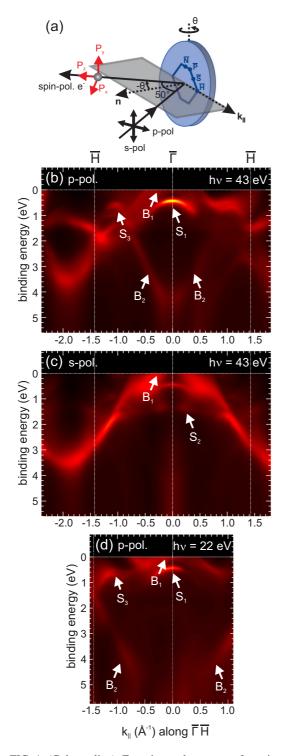


FIG. 1. (Color online) Experimental geometry for spin-resolved ARPES using linearly polarized synchrotron radiation (a). Contour plots of the photoelectron intensities as a function of binding energy and  $\mathbf{k}_{\parallel}$  along  $\overline{\Gamma} \overline{H}$  excited by p- and s-polarized light of hv = 43 eV (b), (c) and by p-polarized light of hv = 22 eV (d).

ARPES spectra were obtained with additional spin detection in the single-channel mode. The energy and angle resolution was 60 meV (40 meV) and  $1.5^{\circ}$  ( $1.5^{\circ}$ ) for 43 eV (22 eV) radiation. The emission angle  $\theta$  of the photoelectrons is defined as positive (negative), when the surface normal is moved away

from (toward) the light propagation vector. All measurements were performed at a sample temperature of 50 K.

The electronic structure of the Ta(110) surface was calculated within density-functional theory, using Perdew-Burke-Ernzerhof generalized gradient exchange-correlation functionals [23,24]. We have applied relativistic multiple-scattering theory as formulated in the Korringa-Kohn-Rostoker (KKR) approach [25,26]. By solving the Dirac equation, spin-orbit coupling is taken into account nonperturbatively. The KKR calculations are complemented by computations with the VASP program package [27,28]. The electronic structures obtained by these independent methods agree very well. The surface relaxation, i.e., the interlayer distances  $d_{ij}$ , were obtained from VASP calculations:  $d_{12} = -4.81\%$ ,  $d_{23} = +0.57\%$ .

The surface systems have been modeled in a semi-infinite geometry. From the KKR Green's function G we compute the spectral density

$$n_l(E, \mathbf{k}_{\parallel}) = -\frac{1}{\pi} \operatorname{Im} \operatorname{Tr} G_{ll}(E + i\eta, \mathbf{k}_{\parallel})$$

of layer l for a small positive  $\eta$ . This quantity is decomposed with respect to angular momentum and spin projection. Spin textures are discussed by means of spin differences  $n_{l\uparrow}(E,\mathbf{k}_{\parallel})-n_{l\downarrow}(E,\mathbf{k}_{\parallel})$ , in which  $\uparrow$  and  $\downarrow$  refer to a specified quantization axis. Surface states are distinguished from surface resonances by tracking their decay toward the bulk: The weight of surface states in the layer-resolved spectral density decays to zero, whereas surface resonances show enhanced weight in the surface region but do not decay to zero toward the bulk because they hybridize with bulk Bloch states.

The experimental ARPES results in Figs. 1(b)-1(d) show the photoelectron intensity as a function of binding energy and  $\mathbf{k}_{\parallel}$  along  $\overline{\Gamma}$   $\overline{H}$ . We observe five pronounced features labeled as  $S_1$ ,  $S_2$ ,  $S_3$ ,  $B_1$ , and  $B_2$ . ARPES results for p- and s-polarized light of  $h\nu=43$  eV [Figs. 1(b) and 1(c)] are compared with measurements for p-polarized light of  $h\nu=22$  eV [Fig. 1(d), data for s-polarized light are not shown].  $S_1$ ,  $S_2$  are identified as surface states, since no photon-energy dependence is observed.  $S_3$  has a small photon-energy dependence and is interpreted as surface resonance. The binding energies of  $B_1$  and  $B_2$  are changing as a function of the photon energy, indicating that these states are related to the bulk continuum.

The spectral density  $n_l(E, \mathbf{k}_{\parallel})$ , shown in Figs. 2(a) and 2(b), was calculated along  $\overline{\Gamma}$   $\overline{H}$  for a bulk and for the topmost surface layer. The bulk spectral density describes the dispersion of  $B_1$  and  $B_2$ . The surface states  $S_1$  and  $S_2$  are found in the surface spectral density. Some high surface-related intensities can be attributed to  $S_3$ . All in all, the spectral intensities describe the ARPES results impressively well and confirm the surface- or bulk-character assignments to the respective states.

The initial-state symmetries and orbital characters for excitation with linear polarized light are summarized in Table I. Neglecting spin-orbit interaction, we can assign even or odd symmetry with respect to the mirror plane for electronic states along  $\overline{\Gamma}\overline{H}$ , i.e., the measuring plane in our experiment (see Fig. 1). Since our experimental data show distinct differences for excitation with s- and p-polarized light, intermixing between even and odd symmetry bands caused by spin-orbit interactions appears to be small. Therefore, we analyze the symmetries in terms of irreducible single-group

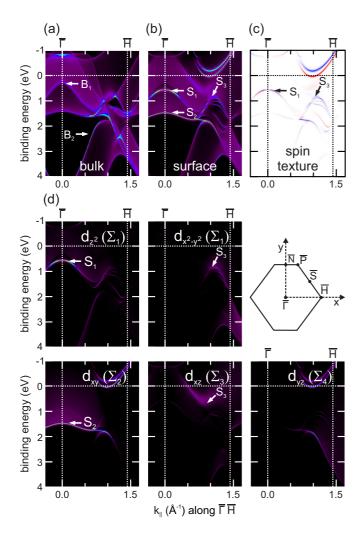


FIG. 2. (Color online) Calculated electronic structure of Ta(110) along  $\overline{\Gamma} \overline{H}$ . Spectral densities  $n_l(E, \mathbf{k}_{\parallel})$  for a bulk layer (a) and for the topmost surface layer (b), sharing a common color scale (dark = small, bright = large values). (c) Difference  $n_{l\uparrow}(E, \mathbf{k}_{\parallel}) - n_{l\downarrow}(E, \mathbf{k}_{\parallel})$  of the spin-projected spectral densities, shown in red (blue) where spin-up (spin-down) intensity exceeds (white denotes zero spin difference). (d) Orbital decomposition of the surface spectral density of (b) with according symmetry representations assigned.

representations  $\Sigma_1$ – $\Sigma_4$  (strictly valid only at  $\overline{\Gamma}$ ). This approximation is supported by the orbital decomposition of the surface spectral density, showing only minor mixing effects [Fig. 2(d)]. On this basis, we are able to interpret the observed surface-related features in more detail.

TABLE I. Initial-state representations for excitation with p- and s-polarized light along  $\overline{\Gamma}\overline{H}$ , according to dipole selection rules neglecting spin-orbit interaction [29].

	Orbital character: Representation
<i>p</i> -polarized (even symmetry)	$s, p_z, d_{z^2}, d_{x^2-y^2}: \Sigma_1 \ p_x, d_{xz}: \Sigma_3$
s-polarized	$p_x, d_{xz}$ . $\Sigma_3$ $d_{xy}$ : $\Sigma_2$ (off-normal)
(odd symmetry)	$p_y,d_{yz}:\Sigma_4$

- (i)  $S_1$  is observed predominantly for p-polarized light. While the undulator provides almost completely p-polarized light, the nominal s-polarized light contains always some p contribution. The small intensity of  $S_1$  for s-polarized light originates largely from this artifact. Therefore, from experiment, we attribute predominantly even symmetry to  $S_1$ . This result is in line with the calculated spectral density for  $S_1$ , which attests almost exclusive  $d_{z^2}$  orbital character.
- (ii)  $S_2$  is only visible in the data for *s*-polarized light with small intensity, but not for *p*-polarized light, therefore it has odd symmetry. The spectral densities reveal  $d_{xy}$  character. Note the vanishing ARPES intensity at  $\overline{\Gamma}$ , where the dipole transition is forbidden.
- (iii) The situation for  $S_3$  is more complex. The spectral features appear predominantly for p-polarized light, while some intensity is also visible for s-polarized light, presumably due to the artifact described above. Our data assign a dominant even symmetry to  $S_3$  in agreement with theory, which predicts surface spectral weight with  $d_{x^2-y^2}$  and  $d_{xz}$  character depending on  $\mathbf{k}_{\parallel}$ . This result nicely confirms earlier theoretical work concluding that  $S_1$  and  $S_3$  are not related [7].

In the following, we focus on the spin dependence of the most dominant feature,  $S_1$ . To unravel the spin character of this  $d_{z^2}$ -like surface state, we have performed spin-resolved ARPES measurements sensitive to all three Cartesian spin components as defined in Fig. 1(a). Please note that the coordinate system for the spin components is rotated by  $\theta$ with respect to that of the sample (defined in Fig. 2; y axis unchanged). Figures 3(b) and 3(c) show spin-resolved spectra for  $-17.5^{\circ} < \theta < 17.5^{\circ}$ , sensitive to the Rashba spin component  $P_y$ . Spin up and spin down are plotted as red and blue. For  $\theta = 0^{\circ}$ , the prominent  $d_{z^2}$ -like surface state  $S_1$  appears at the same binding energy of 0.45 eV for spin up and spin down but with different intensities. Around  $\overline{\Gamma}$  $(|\theta| < 4^{\circ})$ ,  $S_1$  shows a Rashba-type spin-dependent energy splitting of up to 30 meV. The splitting is reversed upon reversal of the emission angle, i.e.,  $\mathbf{k}_{\parallel}$ , while the higher spinup intensity persists. For higher emission angles, additional spin-split features appear, which will not be discussed further. The exclusive Rashba spin polarization of  $S_1$  was tested by measurements sensitive to  $P_x$  [Fig. 3(d)] and  $P_z$  [Fig. 3(e)]. As expected from symmetry considerations, there is no spin polarization along x and z.

To quantify the Rashba behavior of  $S_1$ , we analyzed the spin-resolved data in a limited energy and angle range, obtained with p-polarized light of 43 and 22 eV [Figs. 4(a)and 4(b)]. For both excitation energies the spin splitting is clearly visible. In Fig. 4(c) the energy differences between the two spin channels of  $S_1$  are plotted versus  $\mathbf{k}_{\parallel}$  for both excitation energies. The spin splitting is indeed linear in  $\mathbf{k}_{\parallel}$ , as expected from the Rashba model. From the slope we determined the size of the Rashba parameter  $\alpha$  to  $0.063 \pm 0.007$  eV Å. Our result is in excellent agreement with the calculated value of 0.06 eV Å. Compared with free-electron-like surface states on other high-Z materials, e.g., Au(111), the size of the Rashba parameter is rather small (about 1/5). However, compared to other surface states with localized electrons such as on the lanthanides, this is a rather high value [about two to three times higher than for Tb(0001)].

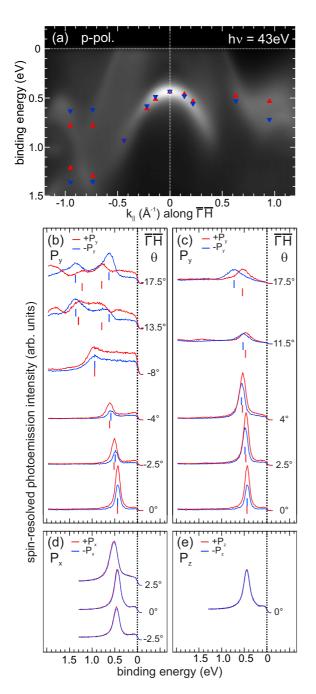


FIG. 3. (Color online) (a) ARPES results for Ta(110) obtained by p-polarized synchrotron radiation with  $h\nu=43$  eV. The contour plot is superimposed by pointing-up and -down triangles, indicating the spin character of the corresponding spectral features, as derived from the spin-resolved spectra in (b) and (c). (b), (c) Spin-resolved ARPES spectra sensitive to  $P_y$  for negative and positive emission angles along  $\overline{\Gamma} \overline{H}$ . Spin-up (spin-down) intensities are marked as red (blue). (d), (e) Spin-resolved ARPES spectra sensitive to  $P_x$  and  $P_z$ .

There is an unexplained detail in the experimental data: the finite spin polarization at normal emission of  $S_1$ . SOC can induce a finite spin polarization of the photoelectrons in highly symmetric setups [15,30,31]. Our experiments show this for the not intrinsically spin-polarized and almost pure  $d_{z^2}$  surface state; that the effect originates from the ARPES measurements is supported by its photon-energy

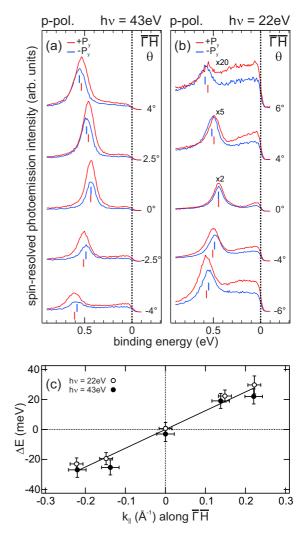


FIG. 4. (Color online) (a), (b) Spin-resolved ARPES spectra of  $S_1$  sensitive to  $P_y$  obtained by p-polarized synchrotron radiation of  $h\nu=43$  and 22 eV. Spin-up (spin-down) intensities are marked as red (blue). (c) Energy difference  $\Delta E$  between spin-up and spin-down intensities of  $S_1$  for  $h\nu=43$  eV (solid dots) and  $h\nu=22$  eV (open dots) as a function of  $\mathbf{k}_{\parallel}$ .

dependence. ARPES calculations in the relativistic one-step model, including the dielectric constant of Ta, confirm the experimental observation.

In conclusion, we proved the influence of SOC on the  $d_{z^2}$  surface state at Ta(110), a state which has no equivalent at W(110). The localized surface state exhibits a Rashba splitting with the highest observed Rashba parameter for  $d_{z^2}$ -like surface states on elemental surfaces so far. Spin-dependent spectral intensities for this highly symmetric unpolarized state could be traced back to SOC effects in ARPES.

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